SYNERGY AND INFORMATION IN COMPLEX NEURAL SYSTEMS

LINKING BIOLOGICAL AND ARTIFICIAL INTELLIGENCE



Pedro A.M. Mediano plogp@pm.me





RESEARCH GOAL

Goal:

Discover the principles of *collective behaviour*.



Behaviour of large groups of agents acting as a whole.









RESEARCH GOAL



Why care about collective behaviour?

To build better systems





To fix it when it breaks



To understand the world



COMMON PRINCIPLE: EMERGENCE



1 Informally: "the whole is more than the sum of its parts."





INTERDISCIPLINARITY AT HEART



RESEARCH OBJECTIVE



THIS TALK

Part I

Theory: Information theory for collective phenomena

Part II

Practice: Data analysis tools, insights, and new results

Part III

What's next: Ongoing research and future outlook

THEORY

ENTROPY AND INFORMATION

► Building block of information theory: Shannon entropy.

$$H(X) = -\sum_{x} p_x \log p_x$$



Entropy is hard to estimate from real data!

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Practical estimator based on Lempel-Ziv's compression algorithm.

PHYSICAL REVIEW LETTERS 127, 124101 (2021)

Decomposing Spectral and Phasic Differences in Nonlinear Features between Datasets
Podro A, M. Mediano^{0,1,*} femando E. Rosso^{0,2,3,4,4} Adam B. Barren^{3,4} and Daniel Bore^{0,1}





Fernando Rosas



Daniel Bor



Adam Barrett



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INFORMATION BEYOND SHANNON

► Shannon's mutual information: from sender to receiver.



But complex systems have many more than two parts!







Plain information theory is insufficient for complex systems!

INSPIRATION FROM NEUROSCIENCE

F Inspiration from neuroscience: Integrated Information Theory (IIT).

Brain dynamics result from two opposing forces:

- Segregation: brain regions can act independently of each other;
- ► Integration: and they can also integrate into high-level cognition.



• Has lead to multiple measures of *integrated information*, Φ .

BEYOND IIT: SYNERGY AND REDUNDANCY

Two variables can either be correlated (i.e. coupled) or not, and this is measured by *mutual information*.



► With 3+ variables there are different types of correlations: some are visible from the parts, some aren't.





Synergy



EXAMPLE: XOR LOGIC GATE



Perfect example of synergy: XOR.



Knowing one input tells you nothing:

$$I(X_1; Y) = I(X_2; Y) = 0$$

Knowing both inputs tells you everything:

$$I(X_1X_2; Y) = 1$$

INTEGRATED INFORMATION THEORY



• First complete, systematic review of Φ measures.



Many measures proposed, still no consensus.



INTEGRATED INFORMATION THEORY



Multiple contributions extending and applying IIT.

 — 18 full-length papers on IIT and related topics in my PhD.



A PRACTICAL MEASURE OF SYNERGY

New measure: O-information, $\Omega(\mathbf{X}^n)$.

Quantifying high-order interdependencies via multivariate extensions of the mutual information

Fernando E. Rosas. Pedro A. M. Mediano, Michael Gastpar, and Henrik J. Jensen Phys. Rev. E 100, 032305 - Published 13 September 2019

redundancy! $\Omega(\mathbf{X}^n) > 0$



synergy!











Imperial College London



Fernando Rosas

Henrik Jensen

Michael Gastpar

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INTEGRATED INFORMATION DECOMPOSITION



Integrated information decomposition:

- Decomposition of Φ into redundant and synergistic components.
- New family of information measures for multivariate data.







nature neuroscience

(IF: 24.9)



Andrea Luppi

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Fernando Rosas



Daniel Bor







SYNERGY IN THE BRAIN



► We calculate the **synergy-redundancy** distribution in the brain.

Synergy higher in areas related with high-level cognitive function. Redundancy higher in areas related with sensorimotor processing.



Synergy minus Redundancy rank gradient

SYNERGY IN NEURAL NETWORKS

► We calculate synergy between layers of small neural nets.

Synergy increases when network learns multiple tasks. **Redundancy** increases when subject to noise (dropout).



LINKING MINDS AND MACHINES



✓ **Redundancy** provides reliable I/O to the system.

 \rightarrow Higher in sensorimotor areas, robust to noise.



CS

FORMALISING CAUSAL EMERGENCE

Informal definition: when 'macro' variable V_t has information about the future not present in 'micro' variables Xⁱ_t.



Tight links between emergence and synergy; tractable emergence lower bounds.



OF SUSSEX

*

- Example of emergence: neural activity during motor control.
- ► Micro variable: 64-channel brain activity.

THEORY

► Macro variable: 3D SVM-decoded hand motion.





WHAT'S NEXT

 $\Psi(V) > 0$

emeraence

Emergence meets art: Synch.Live



Participants move freely, trying to synchronise their hat lights.
 → Real-time feedback by computer vision and online learning.



First-person experience of collective emergence.





Madalina Sas



Hillary Leone Daniel Bor



Fernando Rosas





IMPACT

✓ Fertile ground for new research: 9 MSc + 4 PhD projects based on these theories

- Alexandra Proca Andrew Esterson Connie Sheeran J.C. Farah Hugh Spaughton
- Alberto Liardi Stefan Milhacea Jennifer Fielder Tycho Tax







Andrea Luppi

Hardik Rajpal

uppi Madalina Sas Harc 1 open PhD position in QMUL

✓ Internationally well-received: follow-up research by multiple independent labs.



INT	DOI	DUC	TION
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INTERIM SUMMARY

Theory

- ✓ Significant extensions to information theory for complex systems analysis based on synergy and emergence.
- ✓ New insights linking synergy and redundancy to biological and artificial intelligence.
- ✓ Promising avenues for future research.



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PRACTICE

REAL-WORLD DATA ANALYSIS





Can we apply these ideas to solve real-world problems?



Kes! Let's focus on two examples:

- 1. Mental health treatment.
- 2. Diagnosis of neurological disorders.

PRELIMINARIES: OPEN-SOURCE SOFTWARE

Widely used toolboxes for information-theoretic analyses:



► GPU-accelerated estimation of information measures. → Fastest available estimator of its kind.













G-AUGUST-UNIVERSITÄT **PWOL**

jlizier/jidt pwollstadt/idtxl

Joe Lizier

Patricia Wollstadt

Leo Novelli



APPLICATIONS I: PSYCHEDELIC THERAPY

 Psychedelic drugs have resurfaced as promising treatments for mental health.





2 2011 2012 2013 2014 2015 2016 2017 2018 2019 2020 2021 onature





APPLICATIONS I: PSYCHEDELIC THERAPY



- Entropy-based regressor predicts psychological outcomes of psychedelic therapy. *
 - Prospective patent application.



Taylor Lyons

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APPLICATIONS II: CLINICAL DIAGNOSIS

RARE GENETIC DISEASES

- Angelman syndrome: rare genetic disorder with severe effects.
 - Classifiers with entropy-based features generalise better than previous alternatives.









Joel Frohlich







APPLICATIONS II: CLINICAL DIAGNOSIS



► Some patients have *covert consciousness*, hindering diagnosis.

Emergence-based tools predict unresponsive wakefulness syndrome.



CLOSING THE LOOP: BACK TO ML

RL agent based on information theory learns faster.







Zafeirios Fountas





Karl Friston



Modelling agent interactions helps us understand and train multi-agent systems.









Neil Rabinowitz

Andrea Tacchetti

Francis Song







INTERIM SUMMARY

PRACTICE

- $\checkmark\,$ Demonstration of novel theories implemented and applied on real data.
- ✓ Powerful open-source algorithms for complex systems analysis.
- New insights on real-world problems: neurological diagnosis and mental health treatment.



WHAT'S NEXT

RESEARCH VISION



Future research goals:



- Closer alignment between ML and neuroscience models.
- ✓ Deepen the links between **synergy and learning**.
- Clinical applications in mental health, with direct benefit to patients (e.g. depression).
- ✓ More diverse applications (e.g. economics, social networks).

FUNDING SOURCES



- Multidisciplinarity brings a **diversity of funding streams**. \rightarrow E.g. Engineering, life & physical sciences, mental health.
- Ongoing and upcoming applications:



£ 640.000

JOHN ETON FOUNDATION \$ 230,000





£ 640,000

POSSIBLE INTERNAL COLLABORATIONS

IMPERIAL



Henrik Jensen Department of Mathematics Complexity science



David Erritzoe Department of Brain Sciences Mental health treatment



Tim Evans Department of Physics Complex network analysis



Claudia Clopath Department of Bioengineering Computational neuroscience

POSSIBLE INTERNAL COLLABORATIONS DOC



K Possible collaborative projects:

- ML for neurological diagnosis (BioMedIA)
- Non-Boltzmann entropies for complexity and ML (Yingzhen Li)
- Group dynamics during agent evolution (Antoine Cully)
- Causal emergence and abstraction (Alessandra Russo) \rightarrow More on this in proposed grant application.

Imperial & me



WHY DOC? WHY ME?

- ? Why does my research belong in DoC?
 - ✓ For the rigour and relevance in computing applications to real-world problems.
 - ✓ For the students, who enjoy multidisciplinary projects and courses.
 - ✓ For the required skills, which rely heavily on computing, mathematics, and statistics.
 - ✓ For the opportunities for DoC in terms of funding and collaboration.

WRAP-UP

INTRODUCTION	Theory	PRACTICE	WHAT'S NEXT
	WRA	AP-UP	

- Multidisciplinary computing research spanning information theory, ML, and computational neuroscience, with impactful empirical results.
- ✓ Great research potential, used by several MSc and PhD projects.
- ✓ New funding opportunities beyond usual DoC channels.
- ? Interested? Learn more at:

https://pmediano.gitlab.io

plogp@pm.me

Thank you for listening!

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